Coupling of Charge Regulation and Geometry in Soft Ionizable Molecular Assemblies

Electrostatic Model

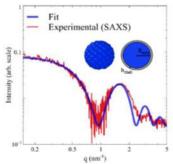
Nonlinear Poisson-Boltzmann $\nabla^2 \Psi(x) = \sinh \Psi$

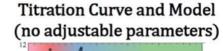
Two boundary conditions

(1)
$$\alpha = \frac{1}{1 + 10^{\text{pH} - \text{pK}_a} \exp \Psi}$$

$$\frac{d\Psi}{dx}\Big|_{x=x_0} = \frac{-4\pi l_B \lambda_D \alpha}{S}$$

Nano-scale structure





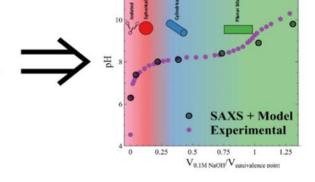


Figure: The theoretical model with its corresponding boundary conditions, along with the particle structures, allows the phase diagram to be determined as a function of pH.

Scientific Achievement

The development of a predictive, parameter-free framework that links molecular charge regulation to self-assembled geometry and environmental conditions.

Significance and Impact

The titration curves and effective charge states demonstrate that pK shifts arise naturally from the coupling between geometry and electrostatics, providing a broadly applicable and physically grounded framework for understanding soft, ionizable materials.

Research Details

 By combining small-angle X-ray scattering experiments with nonlinear electrostatic modeling and simulations, the study shows that structural transitions (e.g., from spherical micelles to cylinders to bilayers) are tightly coupled to ionization behavior.

Joseph M. McCourt, Leticia Lopez-Flores, Sumit Kewalramani, Noah B. Welke, Monica Olvera de la Cruz and Michael J. Bedzyk, J. Phys. Chem. B, 129, 15, 3814–3828 (2025) DOI: https://doi.org/10.1021/acs.jpcb.5c00162



